

# A Peeling Algorithm for Extraction of the HBT Small-Signal Equivalent Circuit

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**Abstract**—Direct extraction is the most accurate method for the determination of equivalent-circuits of heterojunction bipolar transistors (HBTs). The method is based on first determining the parasitic elements and then the intrinsic elements analytically. The accuracy and robustness of the whole algorithm therefore is determined by the quality of the extraction of the extrinsic elements. This paper focuses on a new extraction method for the extrinsic capacitances which have proven to be the main source of uncertainty compared to the other extrinsic parameters. Concerning the intrinsic parameters, all the elements are extracted using exact closed-form equations, including exact expressions for the base–collector capacitances, which model the distributed nature of the base [1]. The expressions for the base–collector capacitances are valid for both the hybrid- $\pi$  and the physics-based T-topology equivalent circuits. Extraction results for InP HBT devices on measured S-parameters up to 100 GHz demonstrate good modeling accuracy.

**Index Terms**—Heterojunction bipolar transistors (HBTs), parameter extraction, small-signal equivalent circuit.

## I. INTRODUCTION

IN THE analysis and design of microwave and millimeter-wave circuits using heterojunction bipolar transistors (HBTs), it is necessary to have an accurate linear equivalent circuit. The last decade has seen an increasing shift from the traditional optimization techniques to the more accurate and simpler direct extraction techniques (see, e.g., [2], [9]–[12] for the T-topology, and [13]–[17] for the hybrid- $\pi$  equivalent circuits). This approach not only simplifies parameter extraction since other methods may be used to accurately determine the bias-independent extrinsic part of the HBT [4]–[6], [13], but it also ensures that the values obtained would be physically related to the actual device/model.

In the complete transistor equivalent circuit the extrinsic capacitances and inductances model the on-wafer coplanar pad structure. Existing methods for determining the pad capacitances, either use the open test structures [13], or the HBT

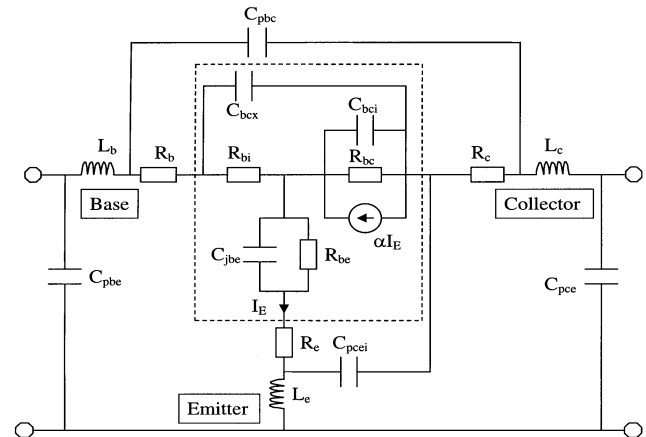


Fig. 1. Small-signal equivalent circuit of the HBT. The dashed box denotes the intrinsic bias-dependent part.

under cutoff operation [4]. However, these methods have been found to be of unsatisfactory accuracy, with the consequence that their values are often guessed or set to zero (see, e.g., [9], [17], [18]). In this paper, a new method for determining these capacitances is suggested. The method, which is based on measurements of a through line, also validates the lumped element model for the coplanar pad structure. Previous work generally considers the coplanar pad structure as consisting of distributed elements, and a consistent lumped-element model still lacks.

Once the parasitic elements are de-embedded, the exact formulation for the seven HBT intrinsic elements (namely,  $R_{bi}$ ,  $C_{bcx}$ ,  $R_{be}$ ,  $C_{be}$ ,  $R_{bc}$ ,  $C_{bci}$ , and  $\alpha$  for the T-topology, or  $R_{bi}$ ,  $C_{bcx}$ ,  $R_{\pi}$ ,  $C_{\pi}$ ,  $R_{bc}$ ,  $C_{bci}$ , and  $G_m$  for the hybrid- $\pi$  equivalent circuits (see Figs. 1 and 2) in terms of the four measured complex S-parameters which was recently presented by the authors is used to complete the extraction [1]. The analytic equations include one for the hitherto unresolved base–collector capacitance  $C_{bcx}$ . In comparison with previously published methods, no simplifying assumptions nor special extra measurements are required for extraction of the entire intrinsic device; and more importantly, each intrinsic equivalent-circuit parameter is extracted at each measured frequency. This formulation is analogous to the method developed for FETs by Dambrine [3].

Extraction of the small-signal equivalent circuit is performed in several steps. In each of the steps, the values of the elements appearing in the outer layer of the circuit are calculated and de-embedded from the measurements, i.e., peeled off from the equivalent circuit. In this extraction scheme, any error in the

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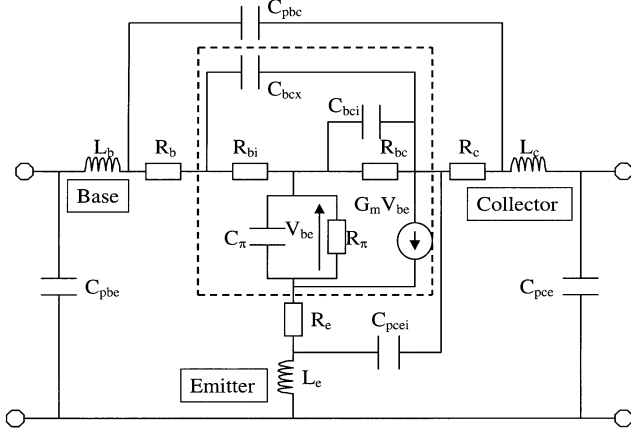


Fig. 2. Hybrid- $\pi$  small-signal equivalent circuit of the HBT. The dashed box denotes the intrinsic bias-dependent part.

values of the elements removed from the circuit would increase the error in the extracted values of the internal circuit elements. Therefore the outer elements of the equivalent circuit must be extracted very accurately in order to obtain a good equivalent circuit.

This paper first gives a description of the new method for determining the pad capacitances. Secondly, the derivation of equations for modeling the intrinsic device at each measured frequency point is given, before outlining the entire extraction procedure. A presentation and discussion of extraction results for InP/GaInAs HBTs conclude the paper. A short section giving approximate, but robust extraction equations for some intrinsic elements is included for comparison purposes.

## II. ANALYSIS

This section gives an analysis of the coplanar environment in which the device is characterized. It also gives a complete analysis for the T-topology. The T-topology, being directly related to device physics, allows checking of the physical relevance of the extracted parameters, and hence is not only useful for circuit design, but also for device optimization and technology development. The hybrid- $\pi$  model is included for completeness, and since it is useful in large-signal modeling [14].

### A. Pad Capacitances

The complete lumped-element equivalent circuit for the HBT appears in Figs. 1 and 2. This circuit includes all of the parasitic elements as well as the internal HBT equivalent circuit elements. As seen in the figures, the first step in the extraction is the removal of the two pad capacitances  $C_{pbe}$  and  $C_{pce}$ . An open test structure [13] and variation of reverse bias across both the HBT junctions [4] have been suggested for determining the pad capacitance values. We, as well as other authors, have found these methods to be inaccurate [17], [18]. Measurement of the test structure assumes an open shunt stub for the complete pad structure while under active operation of the device a substantial part of the pad acts as a shorted transmission line, which, for the short pad lengths, is better modeled by a series inductance.

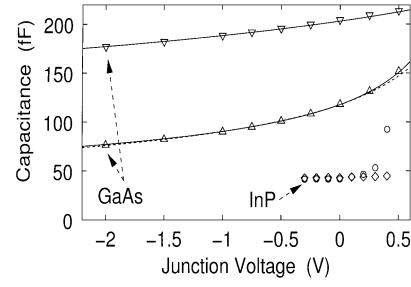


Fig. 3. Example extraction of pad capacitances for GaAs- and InP-HBTs using variation of junction capacitance with reverse bias [4]. GaAs-HBT:  $C_{pbe}$  ( $\nabla$ ),  $C_{pbc}$  ( $\Delta$ ); and InP-HBT:  $C_{pbe}$  (diamonds),  $C_{pbc}$  (o).

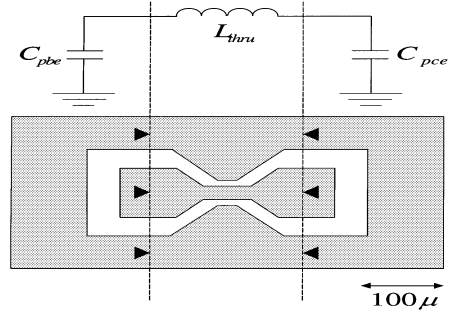


Fig. 4. The through test fixture and its lumped-elements equivalent circuit. The points touched by the RF coplanar probes are marked by arrow heads.

Therefore, the open test structure may overestimate the pad capacitance.

In off-state capacitance measurements, on the other hand, a separation of the pad capacitance from the internal device capacitance is difficult [18]. This is demonstrated in Fig. 3 for a single-finger GaInP/GaAs-HBT and a InP/GaInAs HBT. In case of the GaAs-HBT, the main problem lies in the large values of the measured capacitances. The pad capacitances are given by the small offset that occurs in addition to the pn-junction's capacitances. Thereby, small changes in the other parameters lead to large relative errors in these capacitances. This is demonstrated in Fig. 3. The total base-collector capacitance can be fit well yielding  $C_{pbc} = 12$  fF (solid lines) or  $C_{pbc} = 0$  (dashed lines). For the base-emitter capacitance, only a fit yielding  $C_{pbe} = 0$  is shown. In the case of high-speed InP HBTs the narrow collector and emitter regions are fully depleted even at positive voltages, and the measured capacitances turn out to be constant. Hence, the assumption of bias-dependent intrinsic capacitance and constant pad capacitance is not valid.

We suggest using measurements on a through test fixture as shown in Fig. 4 to extract the pad capacitances. In this structure, a short transmission line between the base and the collector pads replaces the active device. Therefore, the lines conducting current when an active device is connected also conduct current in the test fixture. The lumped-element equivalent circuit for the test fixture is also shown in the figure. The model consists of two capacitances for the open shunt stubs to the left of the left probe and to the right of the right probe and an inductance for the transmission line section between the probes.

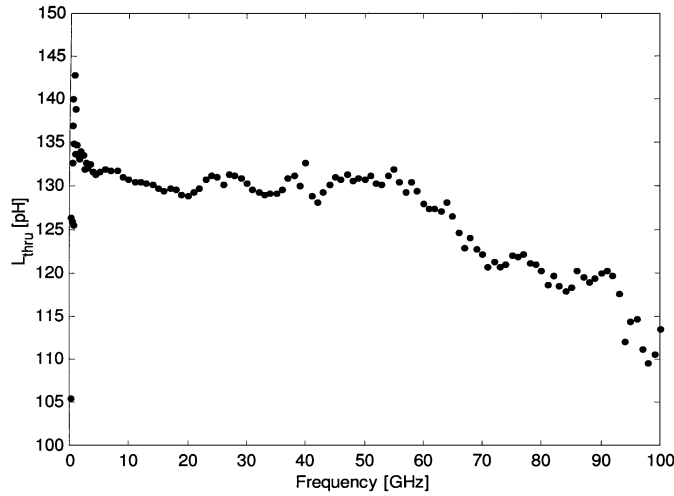


Fig. 5. Measured inductance  $L_{\text{thru}}$  of the through test fixture over the 50-MHz–100-GHz frequency range.

From the  $y$ -parameters of the assumed model for the test fixture the value of the inductance can be found using the following expression:

$$L_{\text{thru}} = -\frac{1}{\omega} \cdot \text{Im} \left( \frac{1}{y_{12}} \right). \quad (1)$$

The inductance extracted from S-parameter measurements of a through test fixture using (1) is shown in Fig. 5. As seen in the figure, the section between the probe tips can be approximated by a lumped value of inductance. For frequencies up to 60 GHz, the value of  $L_{\text{thru}}$  is approximately 132 pH. As the frequency rises, the value of  $L_{\text{thru}}$  decreases because of the skin effect. At a frequency of 100 GHz, the value of  $L_{\text{thru}}$  drops to 110 pH.

The pad capacitance  $C_{pbe}$  can be found by examining the imaginary part of  $1/(\omega \cdot y_{11})$ , which should give the resonance condition for the LC model as

$$\text{Im} \left( \frac{1}{\omega \cdot y_{11}} \right) = \frac{L_{\text{thru}}}{1 - \omega^2 L_{\text{thru}} C_{pbe}}. \quad (2)$$

This function which is shown in Fig. 6 exhibits a resonance at  $\omega_0 = \sqrt{L_{\text{thru}} C_{pbe}}$ . The resonance of the measured test fixture is at a frequency of 89.5 GHz. Using the value for  $L_{\text{thru}}$  from (1) at the resonance frequency, the value of  $C_{pbe}$  is found to be 25 fF.

An alternative expression for  $C_{pbe}$  is

$$C_{pbe} = \frac{1}{\omega} \cdot \text{Im} (y_{11} + y_{21}). \quad (3)$$

Equation (3) gives the same value for  $C_{pbe}$  as that found using the equation for resonance, i.e., (2), and this confirms the validity of the model. Equation (3) can be used to find pad capacitances in measurement systems with a limited frequency range. A similar calculation for  $C_{pce}$  using the resonance frequency of  $\text{Im} (1/\omega \cdot y_{22})$  yields a value of 24.5 fF for the second pad capacitance.

The measurement of the through fixture not only gives accurate values for the capacitances but the fit to the lumped-element model also validates the model used for the pads in the HBT

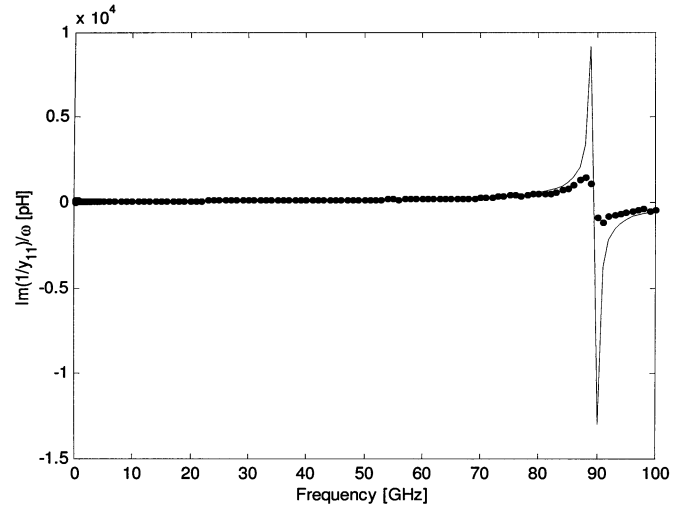


Fig. 6. Measured  $(1/\omega)\text{Im} (1/y_{11})$  data points. A distinct resonance can be observed. The continuous line was calculated from the lumped-elements circuit, assumed lossless.

equivalent circuit. For an accurate extraction, the RF probes should be placed very accurately on the pads. Any displacement of the probes can result in a substantial change of the parasitic inductance. In the setup used in this study, the parasitic inductance was found to be anywhere between 20–80 pH depending on the placement of the probes.

Note that the length of the through test-fixture is approximately twice the length of each pad section for the actual transistor test pads, and therefore the lumped-element model is even more valid for the actual pad structure. The model and fitting extraction results also indicate that capacitive coupling between the input and output ports, i.e.,  $C_{pbc}$ , should be located across the actual device as shown in Figs. 1 and 2, and not across the pad structure as is often done, and, finally, for comparison purposes, the open test structure gives values of pad capacitances that are about 30% higher than those extracted here.

### B. Intrinsic Device

The HBT T-topology equivalent circuit is shown in Fig. 1, with the intrinsic bias-dependent part shown within the dashed box. The internal T-network comprising  $R_{bi}$ ,  $R_{be}$ ,  $C_{be}$ ,  $R_{bc}$ ,  $C_{bci}$ , and  $\alpha$  can be expressed in Z-parameters as follows:

$$[Z_{\text{int}}] = \begin{bmatrix} Z_{11} & Z_{12} \\ Z_{21} & Z_{22} \end{bmatrix} = \begin{bmatrix} R_{bi} + \frac{1}{Y_{be}} & \frac{1}{Y_{be}} \\ \frac{1}{Y_{be}} - \frac{\alpha}{Y_{bc}} & \frac{1}{Y_{be}} + \frac{1}{Y_{bc}}(1 - \alpha) \end{bmatrix} \quad (4)$$

where

$$Y_{be} = \frac{1}{R_{be}} + j\omega C_{be} \quad (5)$$

$$Y_{bc} = \frac{1}{R_{bc}} + j\omega C_{bci} \quad (6)$$

and

$$\alpha = \frac{\alpha_0 e^{-j\omega\tau_1}}{1 + j\omega\tau_2}. \quad (7)$$

$\alpha$  is the common-base high-frequency current gain.  $\alpha_0$  is the dc current gain,  $\tau_1$  essentially models the collector transit time,

whereas  $\tau_2$  models the base transit time as well as the time constants due to the charging of the internal HBT capacitances.

From (4)–(7), it follows that

$$R_{bi} = Z_{11} - Z_{12} \quad (8)$$

$$R_{be} = \frac{1}{\text{Re}(Z_{12})} \quad (9)$$

$$C_{jbe} = \frac{1}{\omega} \text{Im} \left( \frac{1}{Z_{12}} \right) \quad (10)$$

$$R_{bc} = \frac{1}{\text{Re}(Z_{22} - Z_{21})} \quad (11)$$

$$C_{bci} = \frac{1}{\omega} \text{Im} \left( \frac{1}{Z_{22} - Z_{21}} \right) \quad (12)$$

and

$$\alpha = \frac{Z_{12} - Z_{21}}{Z_{22} - Z_{21}} \quad (13)$$

Note that  $\alpha$  may also be computed using

$$\alpha = \frac{Y_{21} - Y_{12}}{Y_{11} + Y_{21}} \quad (14)$$

where  $Y_{ij}$  are the  $Y$ -parameters of the complete intrinsic equivalent circuit. Simple algebraic manipulations show that this equation and (13) for  $\alpha$  are, in fact, completely identical.

Now consider the  $Y$ -parameters of the intrinsic circuit,  $[Y]$ . De-embedding  $C_{bcx}$  gives

$$\begin{aligned} [Y_{\text{int}}] &= [Y] - [Y_{bcx}] \\ &= \begin{bmatrix} Y_{11} & Y_{12} \\ Y_{21} & Y_{22} \end{bmatrix} - \begin{bmatrix} j\omega C_{bcx} & -j\omega C_{bcx} \\ -j\omega C_{bcx} & j\omega C_{bcx} \end{bmatrix} \end{aligned}$$

where  $[Y_{bcx}]$  corresponds to  $C_{bcx}$ .

The inverse of  $[Y_{\text{int}}]$  gives the  $Z$ -parameters of the internal T-network as

$$[Z_{\text{int}}] = \frac{1}{\Delta Y_{\text{int}}} \begin{bmatrix} Y_{22} - j\omega C_{bcx} & -Y_{12} - j\omega C_{bcx} \\ -Y_{21} - j\omega C_{bcx} & Y_{11} - j\omega C_{bcx} \end{bmatrix} \quad (15)$$

where  $\Delta Y_{\text{int}} = \Delta Y - j\omega C_{bcx} \sum Y$  with  $\Delta Y = Y_{11}Y_{22} - Y_{12}Y_{21}$  and  $\sum Y = Y_{11} + Y_{22} + Y_{12} + Y_{21}$

Since (4) and (15) are equal, the intrinsic base resistance  $R_{bi}$  [see (8)] can be expressed as

$$R_{bi} = \frac{Y_{12} + Y_{22}}{\Delta Y - j\omega C_{bcx} \sum Y} \quad (16)$$

and, therefore, we can write

$$\text{Im} \left( \frac{Y_{12} + Y_{22}}{\Delta Y - j\omega C_{bcx} \sum Y} \right) = 0 \quad (17)$$

from which  $C_{bcx}$  is easily determined as

$$C_{bcx} = \frac{1}{\omega} \frac{\text{Re}(Y_s) \text{Im}(\Delta Y) - \text{Im}(Y_s) \text{Re}(\Delta Y)}{\text{Re}(Y_s) \text{Re}(\sum Y) + \text{Im}(Y_s) \text{Im}(\sum Y)} \quad (18)$$

where  $Y_s = Y_{12} + Y_{22}$ .

The time constants and  $\alpha_0$  are calculated as follows. From (7) and (13), taking the reciprocal of the modulus of (7) and squaring both sides of the equation gives

$$\frac{1}{|\alpha(\omega)|^2} = \frac{1}{\alpha_0^2} (1 + \tau_2^2 \omega^2) \quad (19)$$

from which it is clear that plotting  $1/|\alpha(\omega)|^2$  vs.  $\omega^2$  should give a linear graph. The  $1/|\alpha(\omega)|^2$ -intercept gives  $1/\alpha_0^2$  and the gradient gives  $(\tau_2/\alpha_0)^2$  and hence  $\alpha_0$  and  $\tau_2$  can be determined, and, finally,  $\tau_1$  is calculated using

$$\tau_1 = -\frac{1}{\omega} \tan^{-1} \left( \frac{\text{Im}[(1 + j\omega\tau_2)\alpha]}{\text{Re}[(1 + j\omega\tau_2)\alpha]} \right). \quad (20)$$

### C. Hybrid- $\pi$ Model

A similar analysis yields the same equations for  $C_{bcx}$  and  $R_{bi}$  for the hybrid- $\pi$  small-signal equivalent circuit. The equations for extracting the other intrinsic equivalent circuit parameters are identical to those given in [13].

## III. PARAMETER EXTRACTION

The preceding section has outlined a method for obtaining the pad capacitances and the intrinsic HBT using exact formulae. The extraction process starts by determining the pad capacitances  $C_{pbe}$  and  $C_{pce}$  using the through test structure. The series parasitic elements, i.e.,  $L_b$ ,  $L_c$ ,  $L_e$ ,  $R_b$ ,  $R_c$ , and  $R_e$ , are determined from the open-collector measurements as has been done by many other authors, e.g., [4], [6], [17]. Note, however, that de-embedding of  $C_{pbe}$  and  $C_{pce}$  from open collector measurements is important for an accurate extraction of these elements.

The series emitter resistance may also be extracted by the method proposed by Maas [5] which considers the variation of  $\text{Re}(Z_{12})$  with emitter current.  $\text{Re}(Z_{12})$  is essentially constant in the low-frequency range. The capacitance  $C_{pbc}$  is estimated from an open test structure, but since it is small an estimate using the device geometry should be adequate. The capacitance  $C_{pcei}$ , which models the overlapping area of the emitter runners and the collect mesa, is estimated from device geometry. For devices with an airbridge contact to the emitter,  $C_{pcei}$  may be neglected.

The extraction procedure proceeds as follows. First,  $C_{pbe}$  and  $C_{pce}$  are peeled off. Next,  $L_b$ ,  $L_c$ , and  $L_e$  are removed, before peeling off  $C_{pbc}$  and  $C_{pcei}$ . Finally,  $R_b$ ,  $R_c$  and  $R_e$  are removed. The parasitic capacitances are de-embedded from  $Y$ -parameters, whereas the inductances and resistances from  $Z$ -parameters.

Once all the parasitic elements are peeled off from the equivalent circuit, one is left only with measured parameters of the intrinsic device. Next,  $C_{bcx}$  is computed using (18) and also peeled off. All other intrinsic parameters are then calculated using (8)–(13). The transit times and  $\alpha_0$  are evaluated using (19) and (20). A key advantage of calculating each individual element at each measured frequency is that the quality of the extraction can also be checked by looking at any frequency dependence exhibited by the elements. The linear graph used for determining  $\alpha_0$  and the transit times also assists in further checks on the quality of the extraction.

TABLE I  
EXTRACTED EXTRINSIC ELEMENTS.  $C$ 'S IN FEMTOFARADS,  $L$ 'S IN PICOHENRYS, AND  $R$ 'S IN OHMS

$C_{pbe}$	$C_{pbc}$	$C_{pcei}$	$C_{pce}$	$L_b$	$L_c$	$L_e$	$R_b$	$R_c$	$R_e$
(fF)	(fF)	(fF)	(fF)	(pH)	(pH)	(pH)	( $\Omega$ )	( $\Omega$ )	( $\Omega$ )
25	2	3	25	60	65	1.8	2.6	0.85	8.73

TABLE II  
EXTRACTED INTRINSIC ELEMENTS AT  $V_{CE} = 1.5$  V,  $I_C = 8.7$  mA.  $C$ 'S IN FEMTOFARADS,  $R$ 'S IN OHMS, AND  $\tau$  IN PICOSECONDS

$C_{bcx}$	$R_{bi}$	$R_{be}$	$C_{jbe}$	$R_{bc}$	$C_{bci}$	$\tau_1$	$\tau_2$	$\alpha_0$	$f_t$
(fF)	( $\Omega$ )	( $\Omega$ )	(fF)	(k $\Omega$ )	(fF)	(pS)	(pS)		(GHz)
31	15.4	3.4	10	30	5.1	0.37	0.64	0.947	120

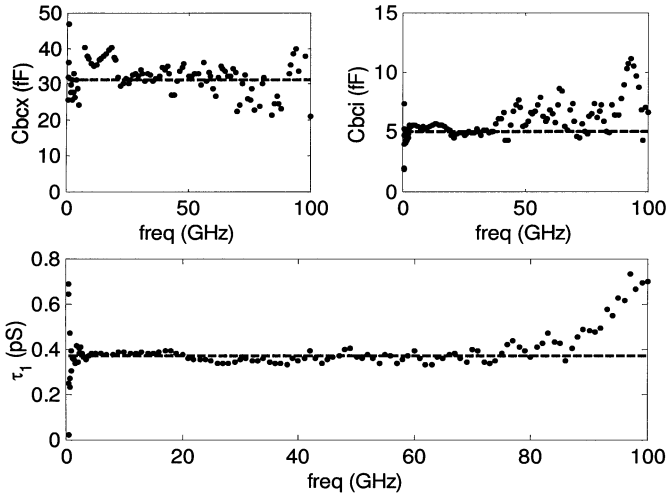


Fig. 7. Extracted  $C_{bcx}$ ,  $C_{bci}$ , and  $\tau_1$  at each measured frequency up to 100 GHz.  $V_{CE} = 1.5$  V,  $I_C = 8.7$  mA. The dashed lines show the average values of the elements.

#### IV. RESULTS AND DISCUSSION

The outlined extraction procedure has been used to extract the parameters of InP/GaInAs HBTs (emitter area  $1 \times 10 \mu\text{m}^2$ ) fabricated in-house at the Technion-Israel Institute of Technology, Haifa, Israel, and which are designed for the millimeter-wave range ( $f_t/f_{\text{max}} = 150/200$  GHz). A frequency-independent base-collector capacitance  $C_{bcx}$  is a good indication that the parasitic elements are accurate, and that the overall extraction is good. This capacitance is relatively independent to errors in emitter resistance and inductance, but sensitive to the other parasitic elements. Errors in  $C_{bcx}$  dramatically influence extracted values of  $R_{bi}$ ,  $R_{be}$  and  $C_{bci}$ . The intrinsic base resistance  $R_{bi}$  is by far the most sensitive element in the extraction procedure, and a frequency-independent value is a sure sign of an excellent extraction.

Tables I and II show the extracted equivalent-circuit elements. As an example, Figs. 7 and 8 show the frequency (in)dependence of some intrinsic elements over the entire measured frequency range. S-parameter fits are shown in Figs. 9 and 10, re-

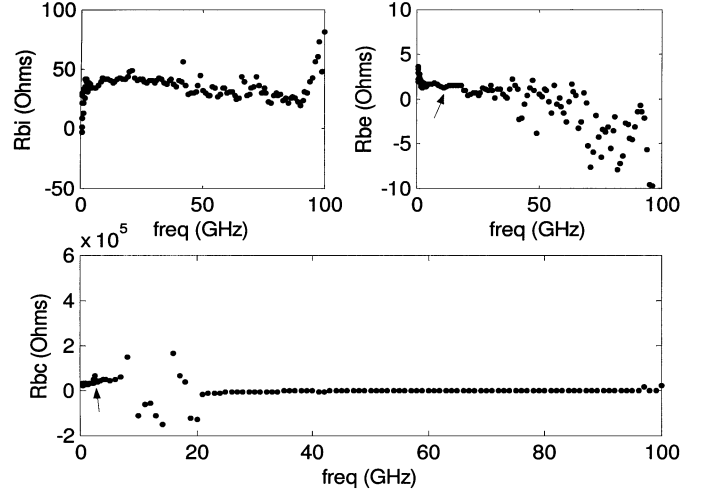


Fig. 8. Extracted  $R_{bi}$ ,  $R_{be}$  and  $R_{bc}$  at each measured frequency up to 100 GHz.  $V_{CE} = 1.5$  V,  $I_C = 8.7$  mA. Arrows point to regions used to extract elements values.  $R_{bi}$  was extracted using [19].

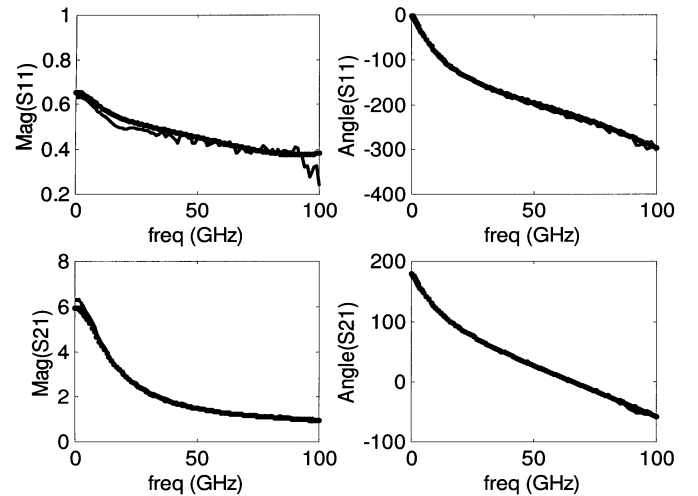


Fig. 9. Measured (-) & simulated (·) S-parameters for the  $1 \times 10$  InP/GaInAs HBT up to 100 GHz.  $V_{CE} = 1.5$  V,  $I_C = 8.7$  mA.

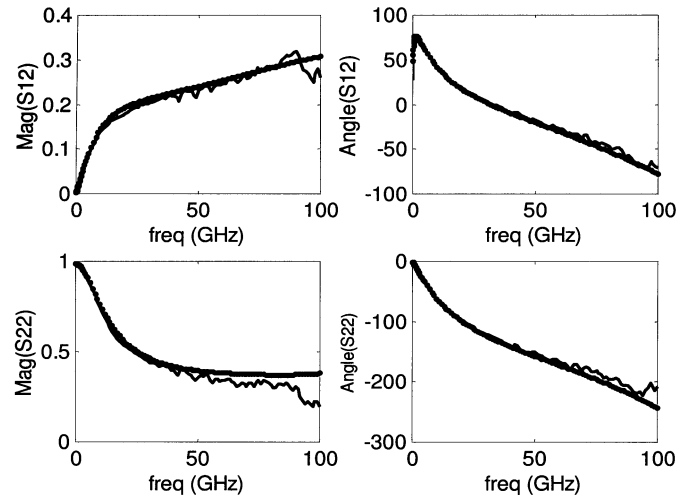


Fig. 10. Measured (-) & simulated (·) S-parameters for the  $1 \times 10$  InP/GaInAs HBT up to 100 GHz.  $V_{CE} = 1.5$  V,  $I_C = 8.7$  mA.

spectively. The errors in the otherwise excellent fits may be attributed to some frequency dependence still shown by  $R_{bi}$  and

TABLE III  
DEVICE GEOMETRY, EXTRACTED BASE–COLLECTOR CAPACITANCES,  $C_{bcx}$   
AND  $C_{bci}$  FOR InP/GaInAs HBT IN THE ACTIVE REGION

Device Dimensions	$C_{bcx}$	$C_{bci}$
emitter, base mesa	(fF)	(fF)
3x10, 7x16.5 $\mu\text{m}^2$	33	11.5
4x10, 8x16.5 $\mu\text{m}^2$	37.5	15.0

$R_{be}$  (see Fig. 8), which indicates existence of residual errors in some parasitic elements. The errors may also be attributed to the pad inductances which show a frequency dependence in the high-frequency range arising from skin effect.

Using synthetic data, the influence of errors in the parasitics on the intrinsic elements was observed in terms of their variation with frequency. For instance, the output resistance  $R_{bc}$  is best taken from the lower frequency range (see Fig. 8 for actual  $R_{bc}$  extraction) since small errors in the parasitic elements cause it to fluctuate much at higher frequencies. The base–emitter junction capacitance  $C_{jbe}$  cannot be distinguished from the base transit time and its extraction remains difficult.

The extracted values of  $C_{bcx}$  and  $C_{bci}$  for  $3 \times 10$  and  $4 \times 10$  devices are shown in Table III, and these agree well with the expected geometric ratio of the emitter mesa area to the (base mesa area–emitter mesa area).

## V. CONCLUSION

A method for determining parasitic pad capacitances using a through test structure has been described. Exact equations for modeling of the intrinsic HBT have also been presented. Small-signal modeling of HBTs is reduced to an accurate determination of the parasitic element values. Extraction results on measurements up to 100 GHz show that the new formulation can be used for reliable and physically meaningful modeling of HBT's. The results also demonstrate that an accurately determined lumped-element equivalent circuit can be used in the millimeter-wave range as well.

## APPENDIX SOME USEFUL EQUATIONS

The modeling concept presented in this paper gives good small-signal models, and this is indirectly confirmed by frequency independence of the intrinsic elements. This section, nonetheless, gives some robust approximate equations which can be used to give a first-hand indication of some intrinsic elements. The equations are valid for the intrinsic equivalent circuit, i.e., measured data which is de-embedded of all parasitics.

The sum of the base–collector capacitances may be approximated from [7], [8]

$$\text{Im} \left( \frac{1}{Z_{22} - Z_{21}} \right) = \omega \left[ C_{bci} + C_{bcx} \left( 1 + \frac{R_{bi}}{R_{bc}} \right) \right] \quad (21)$$

$$\approx \omega (C_{bci} + C_{bcx}) \quad (22)$$

and the intrinsic base resistance  $R_{bi}$  approximated by [19]

$$R_{bi} \approx \text{Re} \left( \frac{1}{Y_{11}} \right) \quad (23)$$

at high frequencies, and, finally, the dynamic emitter resistance  $R_{be}$  by  $\text{Re}(Z_{12})$  at low frequencies.

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